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# Third Semester B.Sc. Degree Examination, March 2021 First Degree Programme under CBCSS

## **Statistics**

# **Complementary Course For Mathematics**

## ST 1331.1 – STATISTICAL DISTRIBUTIONS

(2018 Admission)

Time: 3 Hours

Max. Marks: 80

Use of statistical table and scientific calculator are permitted.

#### SECTION - A

Answer all questions. Each question carries 1 mark.

- 1. What are the parameters of a binomial random variable with mean 4 and variance 3?
- 2. Find the coefficient of variation of Poisson distribution with mean 9.
- 3. If X is a Poisson variable such that P(X = 1) = P(X = 2), obtain P(X = 0).
- 4. If X and Y are independent uniform random variables over [0, 2], determine P(X < Y).
- 5. State the distribution of Z = X + Y, where X and Y are independent standard normal variables.

- 6. Define exponential distribution.
- 7. Define type II beta distribution.
- 8. What do you mean by sampling distribution?
- 9. State the distribution of the ratio of two independent standard normal variables.
- 10. Define statistic.

 $(10 \times 1 = 10 \text{ Marks})$ 

#### SECTION - B

Answer any eight questions. Each question carries 2 marks.

- 11. Define Bernoulli random variable.
- 12. Define hypergeometric distribution.
- 13. The ratio to 3 successes and 4 successes among seven independent Bernoullian trials is  $\frac{1}{4}$ . Find the probability of success.
- 14. If X follow uniform distribution with mean 1 and variance  $\frac{4}{3}$ , find P(X < 0).
- 15. If  $X \sim N(6, 2)$ , find P(1 < X < 3)
- 16. A horizontal line of length 5 units is divided by a point chosen at random into two parts. If the length of the first part is X, find E[X(5-X)].
- 17. What are the advantages of Chebychev's inequality?
- 18. What are the conditions for Lindberg-Levy form of central limit theorem?
- 19. Find the mean of a random variable following chi-square distribution with *n* degrees of freedom.

- 20. A random sample of size 25 is taken from N(1, 9). What is the probability that the sample mean is negative?
- 21. State Bernoulli's weak law of large numbers.
- 22. Let  $X_1, X_2, ...., X_n$  are independent exponential random variables with parameter  $\lambda$ . Show that  $X = X_1 + X_2 + .... + X_n$  follows gamma distribution.

 $(8 \times 2 = 16 \text{ Marks})$ 

#### SECTION - C

Answer any six questions. Each question carries 4 marks.

23. If 
$$X \sim B(n, p)$$
, show that  $Cov\left(\frac{X}{n}, \frac{n-X}{n}\right) = \frac{-pq}{n}$ .

- 24. If X follows Poisson distribution with parameter unity, show that mean deviation about mean is  $\frac{2}{e}$  times the standard deviation.
- 25. If X and Y are independent geometric variables with same parameter, find the conditional distribution of X|X+Y.
- 26. In a normal distribution 30% of the items are above 42 and 30% of the items are below 28. What are the mean and standard deviation of the distribution?
- 27. Derive the moment generating function of normal distribution.
- 28. If X follows beta distribution of the first kind with parameters p and q, show that  $Y = \frac{X}{1-X}$  follow beta distribution of the second kind.
- 29. In a die throwing experiment using an unbiased die, X denotes the number shown by the die. Using Chebychev's inequality, prove that  $P(\mid X-\mu\mid > 2.5) < 0.47$ .

- 30. For a random sample of size 16 from  $N(\mu, \sigma^2)$  population the sample variance is 16. Find a and b such that  $P(a < \sigma^2 < b) = 0.6$ .
- 31. If  $X \sim N(0, 1)$ , prove that  $Y = X^2$  follow chi-square distribution with one degree of freedom.

 $(6 \times 4 = 24 \text{ Marks})$ 

## SECTION - D

Answer any two questions. Each question carries 15 marks.

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Fit a Poisson distribution and calculate the theoretical frequencies.

- 33. State and prove the recurrence relation for central moments of a binomial distribution.
- 34. Derive the expression for central moments of a normal distribution.
- 35. If X is a random variable following F-distribution with  $(n_1, n_2)$  degrees of freedom. Show that  $Y = \frac{1}{X}$  follows F-distribution with  $(n_2, n_1)$  degrees of freedom.

 $(2 \times 15 = 30 \text{ Marks})$