Reg. No.:....

Name : .....

Second Semester B.Sc. Degree Examination, August 2018
First Degree Programme under CBCSS
Complementary Course for Chemistry/Polymer Chemistry
MM 1231.2 : MATHEMATICS – II
Integration, Differential Equations and Analytic Geometry
(2014 Admission Onwards)

Time: 3 Hours

Max. Marks: 80

## SECTION - I

All the first ten questions are compulsory. They carry 1 mark each.

- 1. Define integral curves of a function.
- 2. Suppose that a particle moves so that its velocity at time t is  $v(t) = \sin t \, m/s$ . Find the displacement of the particle during the time interval  $0 \le t \le \frac{\pi}{2}$ .
- 3. Find the points of intersections of the curve  $y = x^2$  and the line y = 3x 2.
- 4. Evaluate  $\int_0^1 \int_0^2 dx dy$ .
- 5. What is the standard equation of the ellipse with center (m, n) and major axis x = m?
- 6. Find the eccentricity of the conic  $r = \frac{3}{2 2\cos\theta}$ .
- 7. Find the order of the differential equation  $\frac{d^2y}{dx^2} + \left(\frac{dy}{dx}\right)^4 \left(\frac{d^3y}{dx^3}\right)^{\frac{1}{2}} = 3y^2.$
- 8. Solve the differential equation  $\frac{dy}{dx} = 1 + y^2$ .
- 9. Find the integrating factor of the differential equation -ydx + xdy = 0.
- 10. Find a particular integral of the differential equation y'' + y = x.



## SECTION - II

Answer any eight questions from among the questions 11 to 22. These questions carry 2 marks each.

11. Evaluate  $\int x^2 \log 2x \, dx$ .

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- Suppose that a particle moves so that its velocity at time t is v(t) = |t 3| m/s. Find
  the displacement and distance travelled by the particle during the time interval
  0 ≤ t ≤ 5.
- 13. Find the area bounded by the x-axis and the parabola  $y = 4 x^2$ .
- 14. Find the volume of the solid generated by revolving the region bounded by the parabola  $y = x^2$  and the line y = 1 about the line y = 1.
- 15. Find the area of the surface that is generated by revolving the portion of the curve  $y = x^3$  between x = 0 and x = 1 about x-axis.
- 16. Find the equation for the ellipse with foci  $(0, \pm 2)$  and major axis with end points  $(0, \pm 4)$ .
- 17. Find the equation of the hyperbola with foci (0,  $\pm$  8) and asymptotes  $y = \pm \frac{4}{3} x$ .
- 18. Solve the differential equation (1 + xy)ydx + (1 xy)xdy = 0.
- 19. Find a general solution for the differential equation y'' + 9y' + 20y = 0.
- 20. Solve the differential equation  $y' + y = e^{-x}$ .
- 21. Find the Wronskian of the functions  $y_1(x) = \cos x$  and  $y_2(x) = \sin x$ .
- 22. Evaluate  $\int_0^a \int_0^x \int_0^y xyz dz dy dx$ .

## SECTION - III

Answer any six questions from among the questions 23 to 31. These questions carry 4 marks each.

23. Solve the initial value problem 
$$\frac{d^2y}{dx^2} = x + \cos x$$
,  $y'(0) = 2$ ,  $y(0) = 1$ .



- 24. Find the length of the astroid  $x = \cos^3 t$ ,  $y = \sin^3 t$ ,  $0 \le t \le 2\pi$ .
- 25. Find the volume of the region bounded by the paraboloid  $z = x^2 + y^2$  and below by the triangle enclosed by the lines y = x, x = 0 and x + y = 2 in the xy-plane.
- 26. Find the value of the double integral  $\int xydxdy$  over the positive quadrant of the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ .
- 27. Derive the standard equation of an ellipse in standard positions.
- 28. Find the center, foci, vertices and directrices of the ellipses  $9x^2 + 25y^2 18x 100y 116 = 0$ .
- 29. Solve the initial value problem  $(x^2 + 1) \frac{dy}{dx} + 4xy = x$ , y(2) = 1.
- 30. Find the orthogonal trajectories of the family of circles  $x^2 + y^2 = c$ .
- 31. Solve the differential equation  $\frac{d^2y}{dx^2} 13\frac{dy}{dx} + 12y = e^{-2x}$  using inverse operator method.

## SECTION - IV

Answer any 2 questions from among the questions 32 to 35. These questions carry 15 marks each.

- 32. a) Find the volume of the paraboloid of revolution  $x^2 + y^2 = 4z$  cut off by the plane z = 4.
  - b) Find the area of the common region that is inside the cardioid  $r = 4 + 4\cos\theta$  and outside the circle r = 6.
- 33. a) Solve the differential equation  $\frac{dy}{dx} + y = xy^3$ .
  - b) Solve the initial value problem y'' y' 2y = 0, y(0) = -4, y'(0) = -17.
  - c) Solve the differential equation  $\frac{d^3y}{dx^3} 5\frac{d^2y}{dx^2} + 7\frac{dy}{dx} 3y = 0$ .



- 34. a) Solve the initial value problem  $y'' 6y' + 13y = 4e^{3x}$ , y(0) = 2, y'(0) = 4.
  - b) Solve the differential equation  $(D^2 + 4D + 4)y = \frac{e^{-2x}}{x^2}$  using method of variation of parameters.
- 35. a) Derive the equation of the tangent to ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  at the point  $(x_0, y_0)$ .
  - b) The Planet Pluto has an eccentricity of 0.249 and a semimajor axis given by a = 39.5 AU.
    - i) Find the equation of its orbit in polar coordinate system if the center of the sun at the pole.
    - ii) Find the period of its orbit.
    - iii) Find its perihelion and aphelion distances.