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Reg. No. :

Name :

Second Semester B.Sc. Degree Examination, May 2020

First Degree Programme under CBCSS

Mathematics

Foundation Course – II

MM 1221 : FOUNDATIONS OF MATHEMATICS

(2018 Admission onwards)

Time : 3 Hours

Max. Marks: 80

J – 2700

SECTION - I

All the first ten questions are compulsory. They carry 1 mark each.

- 1. Define conjunction.
- 2. What is a biconditional statement?
- 3. Define contradiction.
- 4. Give an example of a tautology.
- 5. Prove that empty set is a subset of any set A.
- 6. Find the curve represented by the parametric equation $x = t^2$, $y = t^3$.
- 7. Write the arc length formula for parametric curves.
- 8. Define a parabola.
- 9. Find the distance d between the points (2, 3, -1) and (4, -1, 3).
- 10. Define orthogonal projection of v on e.

SECTION - II

Answer any eight questions from among the questions 11 to 22. These questions carry 2 marks each.

- 11. Find the antecedent and consequent in the following statement. "You can work here only if you have a college degree."
- 12. Determine the truth value of the statement $\forall x \exists y \ni x + y = 3$. Justify.
- 13. Prove that $|x| \ge 0$, $\forall x$.
- 14. Prove that AU(U/A) = U.
- 15. Define injuctive and surjective function. Give example for each.
- 16. If $f(x) = \sin x$ is a function defined on **R**. Find $f([0, \pi])$ and $f([0, 8\pi])$.
- 17. Sketch the curve whose parametric equation is $x = \cos t$, $y = \sin t$.
- 18. Find parametric equations for a circle of radius 2, centered at (3, 5).
- 19. Find the rectangular coordinates of the point *P* whose polar coordinates are $(r, \theta) = (6, 2\pi/3)$.
- 20. Find the unit vector that has the same direction as v = 2i + 2j k.
- 21. Find the angle between the vector u = i 2j + 2k and v = -3i + 6j + 2k.
- 22. Let $u = \langle 1, 2, -2 \rangle$ and $v = \langle 3, 0, 1 \rangle$. Find
 - (a) $u \times v$
 - (b) $\mathbf{v} \times \mathbf{u}$.

SECTION - III

Answer **any six** questions from among the questions 23 to 31. These questions carry **4** marks **each**.

- 23. Prove that "If 7m is an odd number then m is an odd number".
- 24. Which of the following statements are true? Justify
 - (a) If $m^2 > 0$ then m = 0
 - (b) If m > 0 then $m^2 > 0$.
- 25. Prove that $[(p \land \neg q) \Rightarrow c] \Leftrightarrow (p \Rightarrow q)$ is a tautology.
- 26. Find polar coordinates of the point *P* whose rectangular coordinates are $(-2, -2\sqrt{3})$.
- 27. Sketch the graph of $r = \theta(\theta \ge 0)$ in polar coordinates by plotting points.
- 28. State symmetry test.
- 29. State any four rules of vector arithmetic.
- 30. Find the direction cosines of the vector v = 2i 4j + 4k, and approximate the direction angles to the nearest degree.
- 31. Find the angle between a diagonal of a cube and one of its edges.

SECTION - IV

Answer **any two** questions from among the questions 32 to 35. These questions carry **15** marks each.

- 32. Explain in detail any five proof techniques.
- 33. (a) Prove that the subset of a countable set is countable.
 - (b) Prove that the set of all real numbers is uncountable.

- 34. In a disastrous first flight, an experimental paper airplane follows the trajectory of the particle having parametric equation $x = t 3 \sin t$, $y = 4 3 \cos t (t \ge 0)$; but crashes into a wall at time t = 10.
 - (a) At what times was the airplane flying horizontally?
 - (b) At what times was it flying vertically?
- 35. (a) Find the distance D between the point (1, -4, -3) and the plane 2x 3y + 6z = -1.
 - (b) Describe the surface $4x^2 + 4y^2 + z^2 + 8y 4z = -4$.
 - (c) Find equations of the paraboloid $z = x^2 + y^2$ in cylindrical and spherical coordinates.

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