

(Pages : 4)

M – 2362

Reg. No. : .....

Name : .....

Second Semester B.Sc. Degree Examination, December 2021

First Degree Programme Under CBCSS

Mathematics

Complementary Course for Chemistry/Polymer Chemistry

MM 1231.2 : MATHEMATICS – II

INTEGRATION, DIFFERENTIAL EQUATIONS AND ANALYTIC GEOMETRY

(2014-2017 Admissions)

Time : 3 Hours

Max. Marks : 80

SECTION – I

All the **first ten** questions are compulsory. They carry **1** mark each.

1. Evaluate  $\int (\cos x + \sin x) dx$ .
2. Define average -value of a continuous-function  $f$  on an interval  $[a, b]$ .
3. Define arc length of a smooth curve  $y = f(x)$  on the interval  $[a, b]$ .
4. Evaluate  $\int_0^2 \int_0^3 (1+8xy) dx dy$ .
5. Find the order of the differential equation  $(y''')^2 + (y'')^9 + 2y = 6$ .
6. Give the general form of a separable equation.

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7. Write down the auxiliary equation of the differential equation  $y'' - 10y' + 5y = 0$ .
8. Define the conic hyperbola.
9. State reflection property of parabola.
10. State Kepler's first law.

(10 × 1 = 10 Marks)

SECTION – II

Answer **any eight** questions from among the questions 11 to 22. These questions carry 2 marks each.

11. Find the position function of a particle moves with velocity  $v(t) = \cos \pi t$  along a coordinate line, assuming that the particle has coordinate  $s = 4$  at time  $t = 0$ .
12. Find the area of the region bounded above by  $y = x + 6$ , bounded below by  $y = x^2$ , and bounded on the sides by the lines  $x = 0$  and  $x = 2$ .
13. Use a double integral to find the volume of the solid that is bounded above by the plane  $z = 4 - x - y$  and below by the rectangle  $R = [0, 1] \times [0, 2]$ .
14. Use a polar double integral to find the area enclosed by the three-petaled rose  $r = \sin 3\theta$ .
15. Solve  $x(1+y^2)dx + y(1+x^2)dy = 0$ .
16. Solve  $y' + 3y = e^{-2x}$ .
17. Show that the differential equation  $(1+4xy+2y^2)dx + (1+4xy+2x^2)dy = 0$  is exact.
18. Find a general solution of  $y'' + 9y' + 20y = 0$ .
19. Sketch the graph of the parabola  $x^2 = 12y$ .

20. Find the foci of the ellipse  $\frac{x^2}{9} + \frac{y^2}{16} = 1$ .
21. Find the equation of the hyperbola with vertices  $(0, \pm 8)$  and asymptotes  $y = \pm \frac{4}{3}x$ .
22. Find an equation for the parabola that has its vertex at  $(1, 2)$  and its focus  $(4, 2)$ .
- (8 × 2 = 16 Marks)**

SECTION – III

Answer **any six** questions. from among the questions 23 to 31. These questions carry **4** marks each.

23. Suppose that a curve  $y = f(x)$  in the  $xy$ -plane has the property that at each point  $(x, y)$  on the curve, the tangent line has  $x^2$ . Find an equation for the curve given that it passes through the point  $(2, 1)$ .
24. Suppose that a particle moves on a coordinate line so that its velocity at time  $t$  is  $v(t) = (t^2 - 2t) \text{ m/s}$ . Find the distance travelled by the particle during the time interval  $0 \leq t \leq 3$ .
25. Derive the formula for the volume of a sphere of radius  $r$ .
26. Evaluate  $\iint_R xy \, dA$  over the region  $R$  enclosed between  $y = \frac{1}{2}x$ ,  $y = \sqrt{x}$ ,  $x = 2$ , and  $x = 4$ .
27. Evaluate  $\int_0^2 \int_{y/2}^1 e^{x^2} \, dx \, dy$ .
28. Solve  $\cos(x + y)dx + (3y^2 + 2y + \cos(x + y))dy = 0$ .
29. Solve the differential equation  $y'' + 4y' + 4y = 0$ .
30. Solve the differential equation  $y'' + 3y' + 2y = 12x^3$ .
31. Sketch the graph of  $r = \frac{2}{1 - \cos \theta}$  in polar coordinates.

**(6 × 4 = 24 Marks)**

SECTION – IV

Answer **any two** questions from among the questions 32 to 35. These questions carry **15** marks each.

32. (a) Find the area of the region enclosed by  $x = y^2$  and  $y = x - 2$ .
- (b) Use a double integral to find the area of the region  $R$  enclosed between the parabola  $y = \frac{1}{2}x^2$  and the line  $y = 2x$ .
33. (a) Find the arc length of the curve  $y = x^{3/2}$  from  $(1,1)$  to  $(2, 2\sqrt{2})$ .
- (b) Find the area of the surface that is generated by revolving the portion of the curve  $y =$  between  $x = 1$  and  $x = 2$  about the  $y$  - axis.
34. Solve the following differential equations
- (a)  $y'' + 5y' + 4y = 10e^{-3x}$
- (b)  $4'' + 4' + 4y = e^{-x} \cos x$ .
35. Sketch the graphs of the hyperbolas
- (a)  $\frac{x^2}{4} - \frac{y^2}{9} = 1$
- (b)  $y^2 - x^2 = 1$ .

(2 × 15 = 30 Marks)